## Worksheet

Students number

grade

Students name

Omar extended his method to solve any third-degree equations for positive roots. He discussed nineteen types of cubic equations ( expressed with only positive coefficients ). Each of the remaining fourteen he solved by means of conic sections. It is possible to classify these fourteen cubics, using modern notation ( CARDAN 1501-1576 ). To illustrate this reduction , take a cubic of the form

 $Z^3 + PZ^2 + qZ + r = 0$ 

where the coefficients p, q and r can be positive, negative or zero.

Setting  $Z = x - \frac{p}{3}$  in the above equation of the form  $x^3 + bx = a$ . Calculate------